Dynamic modulation of local population activity by rhythm phase in human occipital cortex during a visual search task

Kai J. Miller1,2,3,4,*, Dora Hermes5, Christopher J. Honey6, Mohit Sharma7, Rajesh P. N. Rao1,8, Marcel den Nijs7, Eberhard E. Fetz1,9, Terrence J. Sejnowski10, Adam O. Hebb3, Jeffrey G. Ojemann3, Scott Makeig11 and Eric C. Leuthardt12

Brain rhythms are more than just passive phenomena in visual cortex. For the first time, we show that the physiology underlying brain rhythms actively suppresses and releases cortical areas on a second-to-second basis during visual processing. Furthermore, their influence is specific at the scale of individual gyri. We quantified the interaction between broadband spectral change and brain rhythms on a second-to-second basis in electrocorticographic (ECoG) measurement of brain surface potentials in five human subjects during a visual search task. Comparison of visual search epochs with a blank screen baseline revealed changes in the raw potential, the amplitude of rhythmic activity, and in the decoupled broadband spectral amplitude. We present new methods to characterize the intensity and preferred phase of coupling between broadband power and band-limited rhythms, and to estimate the magnitude of rhythm-to-broadband modulation on a trial-by-trial basis. These tools revealed numerous coupling motifs between the phase of low-frequency (δ, θ, α, β, and γ band) rhythms and the amplitude of broadband spectral change. In the θ and β ranges, the coupling of phase to broadband change is dynamic during visual processing, decreasing in some occipital areas and increasing in others, in a gyraly specific pattern. Finally, we demonstrate that the rhythms interact with one another across frequency ranges, and across cortical sites.

Keywords: electrocorticography, occipital cortex, vision, broadband, rhythm, phase–amplitude coupling, nested oscillation, beta

INTRODUCTION

Recent electrocorticographic (ECoG) and local field potential (LFP) measurements have revealed a link between neuronal population activity and changes in broadband spectral power in the brain surface electric potential (Manning et al., 2009; Miller et al., 2009b; Whittingstall and Logothetis, 2009). This broadband change has been studied primarily by examining power at higher frequencies, where underlying brain rhythms (δ, θ, α, β, and low-γ) do not obscure behaviorally-modulated broadband changes (Brindley and Craggs, 1972; Crone et al., 2001; Edwards et al., 2009; Miller et al., 2009a, 2010a; Jacobs and Kahana, 2010), and more recently by decomposition of spectral changes to remove the rhythms (Miller et al., 2009c). These brain rhythms have long been known to fluctuate with behavior (Beck, 1891), but whether they reflect an active or passive agent in cortical computation has not been directly addressed until recently. Recent measurements have demonstrated that the phase of low-frequency rhythms modulates the amplitude of high frequency power in ECoG (Mormann et al., 2005; Canolty et al., 2006; Osipova et al., 2008; Penny et al., 2008; He et al., 2010). This finding implies that the physiological mechanisms underlying a particular brain rhythm are influencing neuronal population activity recorded at the cortical surface, and further investigation may therefore yield insight into large-scale information processing motifs in the brain. These previous studies have focused on phase modulation of broadband amplitudes on the timescale of minutes. The examination of modulation at finer temporal resolution may reveal how information is dynamically processed in the brain on the timescale at which neural circuits engage and disengage with transient stimuli.

With a single exception (He et al., 2010), previous reports of these types of nested oscillations have focused on coupling between the phase of a low-frequency rhythm and a “high-gamma” range (Mormann et al., 2005; Canolty et al., 2006; Osipova et al., 2008; Penny et al., 2008; Cohen et al., 2009). Close inspection of the figures...
in these manuscripts indicates that this “high-gamma” may be a reflection of broadband change, and not a band-limited γ-rhythm. It is important to draw a distinction between broad band activity and higher frequency γ-rhythm (>50 Hz) amplitude changes as they may reflect distinct underlying physiologic phenomena. The γ-rhythm has been suggested to play a role in active computation in the brain by synchronization – associating distinct cortical sites coherently to facilitate computation (Singer, 1993; Fries et al., 2001; Womelsdorf et al., 2005, 2007; Siegel et al., 2008; Mitchell et al., 2009). In contrast to playing a specific computational role, the broadband power measured at an electrode reflects the average spike rate of the neurons that project to the local neuronal population of roughly 5 × 10^6 neurons in the gray matter beneath each electrode (Manning et al., 2009; Miller et al., 2009b; Miller, 2010). Any phenomena that are observed in the aggregate potential therefore reflect the general activity of this underlying population.

Universal functional properties are often attributed to band-limited rhythmic phenomena. In some cases, this might be biologically plausible – the θ rhythm, for example, may enable a central hippocampal mechanism to coordinate a distributed neocortical network during planning and memory retrieval (Mormann et al., 2005; Canolty et al., 2006; Tort et al., 2009). The α rhythm may reflect suppressive synchronization across visual cortex when there is no visual input at all (Osipova et al., 2008), and therefore not a major feature of our task (as described below), where the subjects’ eyes were open throughout both visual search and ISI epochs. Emerging experimental results suggest that the α-rhythm may not emerge as a large-scale brain feature in visual cortex until the signal is averaged over the larger spatial scales associated with EEG and MEG recordings (Edwards, 2010, Personal Communication).

In this article, we lay out a general framework for examining modulation of local population activity by low-frequency rhythms in the brain. A “phase-coupling palette” is constructed to visualize the full range of coupling across a wide range of frequencies. We isolate particular frequency ranges, and demonstrate how trial-by-trial modulation can be quantified in a robust way using the “phase-coupling vector.” These measures reveal numerous coupling motifs between low-frequency rhythms and broadband spectral change in human occipital cortex. This coupling changes dramatically on a trial-by-trial basis as individuals switch between engagement in a visual search task and fixation on a blank screen. Our findings suggest that rhythms have multiple influences, facilitating and suppressing the activity of cortical populations of neurons. Within a specific frequency range, these influences can be gyrally specific, releasing one area during visual engagement, while actively suppressing another.

**METHODS**

**SUBJECTS**

All five subjects in the study were epileptic patients at Harborview Hospital in Seattle, WA. Sub-dural grids and strips of platinum electrodes were clinically placed over frontal, parietal, temporal, and occipital cortex for extended clinical monitoring and localization of seizure foci. Each subject gave informed consent to participate in an Institutional Review Board approved experimental protocol. All patient data was anonymized according to IRB protocol, in accordance with HIPAA mandate.

**RECORDINGS**

Experiments were performed at the bedside, using Synamps2 amplifiers (Neuroscan, El Paso, TX, USA) in parallel with clinical recording. Stimuli were presented with a monitor at the bedside using the general purpose BCI2000 stimulus and acquisition program (interacting with proprietary Neuroscan software), which also recorded the behavioral parameters and cortical data. Sub-dural platinum electrode arrays (Ad-Tech, Racine, WI, USA) were arranged as combinations of 8 × [4, 6, 8] rectangular fronto-temporo-parietal arrays and 1 × [4, 6, 8] linear temporal and occipital strips. The electrodes had 4 mm diameter (2.3 mm exposed), 1 cm inter-electrode distance, and were embedded in silastic. The potentials were sampled at 1000 Hz, with respect to a scalp reference and ground (Figure 1A). These signals had an instrument-imposed band-pass filter from 0.15 to 200 Hz.

**VISUAL SEARCH TASK**

Subjects participated in a visual search task presented on a LCD monitor ~1 m away, in which 2 s visual search stimuli were interleaved with 2 s inter-stimulus-intervals (ISIs) during which the screen was blank. Each visual search stimulus (e.g., Figure 1B) consisted of three parts: (1) a 5-row by 4-column array of colored boxes (~1 cm by 1 cm), (2) a white star positioned in the center of one of these boxes, and (3) a black arrow (~2 cm by 1 cm) centered ~1.5 cm to the right of the right-most box in the middle row. In each visual search stimulus, the star appeared randomly in one of the colored boxes, and the arrow pointed randomly in one of four cardinal directions (“right,” “left,” “up,” or “down”). The subjects’ task was to state the color of the box that was adjacent to the star in the direction of the arrow. Since fixation was not constrained, and eye position was not measured, we cannot know whether differential effects between different arrow directions were due to attention or a late visual microsaccade between the star and the arrow, or different box position. It seems unlikely that we are measuring “motor processing” in visual cortex during visual search, but we cannot exclude this possibility. Because the uncertainty about attention versus gaze-shift-driven neural activity limits our ability to examine the functional subcomponent of visual processing, the present study is agnostic to these distinctions, and is focused on the generic relationship between brain rhythms and cortical visual processing.

**ELECTRODE LOCALIZATION**

Cortical surface mesh reconstructions were made using preoperative structural MRI. Electrode positions were calculated with respect to the structural MRI from post-operative computed tomography (CT) using the CTMR package of Hermes et al. (2010). When the MRI or CT was of insufficient quality, hybrid techniques involving x-ray were employed to obtain cortical rendering and/or electrode position (Miller et al., 2010b).

**SIGNAL PROCESSING**

Complex signals \( \tilde{V}(f,t) = r(f,t)e^{i\phi(f,t)} \) at discrete frequencies, \( f \), were extracted from the raw potential using Morlet wavelets, and complex signals representing a range of frequencies \( \tilde{V}(f,t) = r(F,t)e^{i\phi(F)} \) were generated using a band-pass and then the Hilbert transform. The log of the decoupled broadband amplitude, \( \chi(t) \), was also
extracted from the raw potential, using the approach outlined in Miller et al. (2009c). The methods for pre-processing, and other pre-established signal processing, are detailed in the Methodological Appendix. Synthetic data were generated to validate the signal processing approach, and the methods to do this are also detailed in the Appendix.

**BROADBAND COUPLING TO LOW-FREQUENCY PHASE (ILLUSTRATED IN FIGURE 10–F)**

The coupling was estimated by calculating the average log-broadband amplitude $\chi(t)$ as a function of the rhythm phase $\phi$ in small phase intervals,

$$\chi_k = \langle \chi(t) \rangle_{\phi \equiv \phi_k^{\mod} \equiv \phi_k^{\mod} / \pi}$$

where $k' = k - K/2$ ($K$ total intervals). For example, for $K = 24$ (the number used in these analyses), then $\chi_k$ represents the mean log-broadband when the phase of the low-frequency rhythm is in the interval between 0 and $\pi/12$. The center of each interval is denoted $\phi_k$, so $\phi_{12} = \pi/24$. To get a full picture of the strength and preferred phase of coupling across a range of frequencies, the wavelet-obtained rhythms at each frequency are used to build up a “palette” of $\chi$ at each frequency. This has an advantage in that ranges of coupling and distinct coupling to different rhythms are revealed, in many cases, as separate phenomena, because there are different preferred phases of coupling.

**THE COUPLING VECTOR AND TRIAL-BY-TRIAL STATISTICS (ILLUSTRATED IN FIGURE 2)**

To condense the range of frequencies composing a given rhythm into one measure, the Hilbert transform was applied, with frequency range chosen based upon inspection of the palette. This allows for the calculation of a “coupling vector” by taking the dot-product $Z_{\mod} e^{i\phi} = 1/K \sum_k \chi_k e^{i\phi_k}$. $Z_{\mod}$ is the magnitude of coupling between phase of the rhythm and the log-broadband amplitude (because we $z$-score $\chi(t)$, $Z_{\mod}$ is roughly the amount of variation in the $z$-score that correlates with the phase of the rhythm concerned), and $\phi$ is the preferred phase of this interaction. This can be calculated on a trial-by-trial basis, breaking up the data into smaller epochs (2 s trials in our case) and calculating a coupling vector for each trial. To assess the distribution of coupling for $N$ trials of a given type, one cannot simply compare the contribution of trial $n$ to the distribution of coupling values as $Z_{\mod(n)}$ because if $\phi$ is not reproducible from trial-to-trial, then $Z_{\mod(n)}$ can be a large value even on trials in which the coupling preferred phase is opposite to that of the majority of other trials in the distribution. In other words, the fact that $Z_{\mod(n)}$ must be non-negative would strongly bias the distribution of $Z_{\mod}$ values so that the mean of the distribution can be significantly greater than zero even when there would be no underlying coupling of consistent phase. For this reason, the distribution of values $Z'_{\mod(n)} = Z_{\mod(n)} \ast \cos(\phi(n) - \phi^*)$ is used, where $\phi^*$ is the preferred phase of the mean coupling vector for trials of type $q$: $Z'_{\mod} e^{i\phi^*} = 1/N \sum_n Z_{\mod(n)} e^{i\phi(n)}$. The quantity $Z'_{\mod}$ can be negative or positive and can therefore have a distribution significantly overlapping with zero (indicating an absence of reliable phase modulation). For each type of trial, the distribution of coupling can be assessed using the distribution $Z'_{\mod(n)}$. We demonstrate the significance of these measures using error bars which represent three times the standard error of the mean. Note that if all trials are of type $q$, then the average coupling vector across trials is the same as the coupling vector of the full timeseries. This method has an advantage over the “large-time shift” bootstrapping approach (Penny et al., 2008) because the data may be segregated into smaller time trials, and statistics may be computed by comparing the distribution of values for trials of one behavioral state versus trials of a different behavioral state. It may also be used to compare discontinuous trials of one type (or all trials concatenated) versus 0. This allows us to examine significant shifts in phase–amplitude coupling during different trial types (where $q =$ “ISI,” versus $q =$ “right,” etc.) and also to assess the significance of each independently versus zero. One might in principle look for shifts in the distribution of preferred phase, but this is only meaningful in the case that significant coupling versus zero has been established independently for each of the two distributions. We defer examination of task-related shift in preferred phase to future studies.

**CROSS-RHYTHM INTERACTION**

We also calculated the interaction between the 4–8 Hilbert phase $\phi(4–8 \text{ Hz}, t)$, and the 12–20 Hz analytic amplitude $r(12–20 \text{ Hz}, t)$. This was done in the exact same fashion as for the $\phi$ to $\chi$ comparison, replacing $\chi$ with $r(12–20 \text{ Hz}, t)$. There are many such inter-rhythm interactions (e.g., Lakatos et al., 2005; Osipova et al., 2008; Cohen et al., 2009; Tort et al., 2009), but we defer further explorations of these to future studies.

**RESULTS**

**TASK-SPECIFIC CHANGES IN THE RAW POTENTIAL, THE AMPLITUDE OF RHYTHMS, AND IN DECOUPLED LOG-BROADBAND SPECTRAL CHANGE BETWEEN VISUAL SEARCH AND INTER-STIMULUS INTERVAL EPOCHS**

**Averaged power spectra**

The averaged power spectral density (PSD) during visual engagement and ISI exhibits a general 1/f shape, with superimposed rhythms that deviate from this 1/f structure at particular frequencies. During behavior, these averaged PSDs most commonly reveal decreases in power in the classic $\theta (\sim 4–8 \text{ Hz})$, $\alpha (\sim 8–12 \text{ Hz})$, and $\beta (\sim 12–20 \text{ Hz})$ rhythms during visual engagement, and increases in power in the $\gamma$ rhythm (30–50 Hz), and in broadband change (Figures 1C and 4H, I).

**Dynamic power spectra**

The dynamic spectra shown in Figures 4 and 5 reveal that there are both broadband spectral changes, and corresponding increases and decreases in the $\theta/\alpha/\beta/\gamma$ ranges associated with the onset of visual search stimuli.

**Decoupling the cortical power spectrum**

A principal component decomposition of the PSD clustered rhythmic, spectrally peaked, phenomena in the 2nd to 4th principal components (Figure 1C). Reconstruction of the PSD without these components revealed broadband spectral change, across the entire frequency domain, with an approximately 1/f structure. This broadband phenomenon is distinct from a higher $\gamma$-rhythm occurring as a peaked activity at 50 Hz and above (see Figures 4H, I).
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throughout the entire visual search task, and most strongly so at cue onset (Figures 4 and 5). In other areas, such as portions of the lingual gyrus, this phenomenon is suppressed (Figure 5H). This broadband measure is a robust correlate of local cortical activity (Manning et al., 2009; Miller et al., 2009b,c; Miller, 2010) and its modulation by the phase of low-frequency rhythms is the focus of this paper.

**Extraction of time-varying broadband change**

A time-varying estimate of broadband spectral change was obtained by projecting the dynamic spectrum into the first principal spectral component (Figure 1D). The broadband change approximates the time-varying amplitude function $A(t)$ in the power-law relationship: $P(t) \sim A(t)(1/f)^\alpha$. In early visual areas of the occipital cortex (peri-calcarine and occipital pole), this phenomenon is augmented (here shown smoothed). In this illustration, the 5 Hz portion of the signal is extracted using a 5 Hz Morlet wavelet (here colored for phase – red denotes surface-positive, and green denotes surface-negative). The timeseries of the log of the broadband is shown, colored by coincident phase of the 5 Hz signal. (E) The timeseries of the log of the broadband is sorted by the coincident phase of the 5 Hz signal. (F) The average of the log-broadband amplitude ($Z$-score units, denoted $\chi_k$ in the Methods) for each 5 Hz phase is shown, with errorbars denoting three times the standard error of the mean (3*SEM) for each phase. This can be appreciated in one dimension as the “5 Hz coupling row.” (G) The process detailed in (D)–(F) is repeated at each frequency from 1 to 50 Hz, to obtain a full coupling palette, and to illustrate how the full range of low-frequency rhythms modulates local brain activity (as captured by broadband spectral change).
Event-related potentials
The event-related potentials reveal characteristic voltage deflections at the onset and offset of visual stimuli. These were transient and non-specific, and present whether the corresponding broadband signal increased or decreased (Figures 4 and 5).

Trial-by-trial amplitude measures
The average and 3*SEM amplitudes of epoch-averaged broadband change reveal both increases and decreases (Figures 4 and 5) during visual search periods when compared with ISI epochs. Early visual areas show characteristic increases in power, while other areas show decrease. As shown in Figure 4, these trends cluster by gyral location. Amplitudes of the 12–20 Hz amplitude (Figures 4 and 5) also reveal both task-related increases and decreases in amplitude during visual search engagement, but these are not linked to broadband change in any simple way. There is task-related increase in the 4–8 Hz amplitude (Figure 5) – although this phenomenon was not universal across subjects nor brain area.

THERE ARE NUMEROUS COUPLING MOTIFS BETWEEN LOW-FREQUENCY RHYTHMS AND BROADBAND SPECTRAL CHANGE
Figure 1 demonstrates that robust modulation of broadband power can be identified across a range of different frequencies by visualizing palettes of rhythm-to-broadband coupling. These palettes display the range of frequencies that are coupled, and the predominant phase of this coupling. Figure 3 shows a strong and significant modulation of broadband spectral change with the phase of low-frequency rhythms in the δ/θ/α/β/γ ranges, and the relative magnitude of each change at different sites in occipital cortex. These modulatory rhythms often superimpose at the same cortical sites, and can often be appreciated as separate phenomena by the different preferred phase of coupling.

- δ (~1–3 Hz) most often has a preferred coupling phase of −π/4 to −π/2, although there are clear exceptions in subjects 4 and 5 (left-most lower palette in Figures 3 and 4D) where the preferred phase is π.
- θ (~4–8 Hz) has a preferred coupling phase of π which appears robustly across subjects and electrodes. (Although Figure 4G is a notable exception in this and other rhythm cases).
- α (~8–12 Hz) most often has a preferred coupling phase of π/2 to 3π/4, although this is not universal.
- β (~12–20 Hz, “low-β” although particular range appears variable between sites) most often has a preferred coupling phase of 3π/4. There are notable exceptions to this (Figure 3 – row 4, column 2; Figure 4G).
- “Canonical γ” (30–50 Hz) coupling is observed in Figures 2–4 with various preferred phases.

It is possible that, in some cases, the smooth, continuous, “diagonal bands” visible in the lower frequencies of the phase-coupling palettes (δ, θ, α bands) may not reflect a set of distinct couplings between band-limited low-frequency rhythms and broadband power. Instead, they may reflect a process in which broadband power is elevated at a fixed time lag relative to the peak of the voltage trace, and this fixed time lag then appears as a continuously varying phase lag across different low-frequency bands.

THE AMPLITUDES AND PHASES OF RHYTHMS IN ADJACENT CORTICAL SITES ARE CORRELATED WITH ONE ANOTHER
As shown in Figure 4J, the phase coherence in the 12–20 Hz range is strong and significant in adjacent sites throughout the 7-electrode strip for subject 5 (note that this is not simply a result of re-referencing, because 63 electrode sites contributed to the common average, not just the 7 shown). This coherence is significant throughout, but is less during visual search task – which might partially be a product of the lower rhythm amplitude in a noise-like background. The coherence is sustained better across neighboring electrodes on the same gyrus. The correlation in the time course of the amplitude of the rhythms in adjacent electrodes is also significant (Figure 4K), and is significantly increased during visual search engagement in only three co-gyrus electrodes (Figures 4B–D).

THE BROADBAND AMPLITUDE IS SIGNIFICANTLY MODULATED BY THE PHASE OF LOW-FREQUENCY RHYTHMS
When the potential time series is separated into behaviorally relevant epochs (as described in Figure 3), there is significant modulation during both visual search cues and inter-stimulus intervals. This is shown explicitly for a 4–8 Hz band and a 12–20 Hz band (Figures 4 and 5).

THE MODULATION OF BROADBAND POWER BY RHYTHM PHASE SHOWS TASK-DEPENDENT INCREASES AND DECREASES
The 12–20 Hz range simultaneously shows both increases and decreases in modulation with engagement in the visual search task, and these patterns cluster gyraly (Figures 4 and 5). The visual search induced modulation decreases are most often associated with “active” brain areas, where broadband power increases during visual search.

THE PHASE OF ONE RHYTHM CAN ALSO MODULATE THE AMPLITUDE OF ANOTHER, IN A TASK-DEPENDENT MANNER
In each subject, modulation of the 12–20 Hz amplitude by the 4–8 Hz phase was observed, and changed during visual search in some cases (Figures 5 and 6). Such inter-rhythm modulation appeared in at least one site in every subject, but was not present in most sites.

SIMULATED DATA SUPPORTS SIGNAL PROCESSING APPROACH
A heuristic model was used to create synthetic data with broadband 1/f properties and modulation by a rhythmic input (Figures 7 and 8). This synthetic data was naively separated by the data analysis methods used on cortical data. The resulting spectra, palette, and modulation measures clearly resemble those found from recorded brain signals. When a negative control was analyzed (Figure 9), there is a complete lack of coupling structure.

DISCUSSION
Our most significant and novel finding is that local cortical activity is dynamically modulated by the phase of different brain rhythms, tracking cognitive engagement on a second-to-second basis for specific cortical sites. In the occipital cortex this modulation was most pronounced in the θ (4–8 Hz) and β (12–20 Hz) ranges during periods of relative cognitive disengagement and dissolves during engagement in a visual search task. This relative increase
instantaneous firing rate of many neurons simultaneously. This is consistent with coarse-graining of phenomena at the single-neuron scale, where the timing of individual action potentials is preferentially locked to a specific phase of ongoing local field potential oscillations (“spike-field coupling” – Buzsaki and Draguhn, 2004). Thus, ECoG rhythm phase to broadband amplitude findings, such as those reported in this study, may reveal a population-averaged reflection of this spike-field coupling. Because these experimental results imply that rhythms are modulating the activity of whole neuronal populations, a distinction must be drawn between fluctuations in rhythmic modulation and amplitude in a rhythm. For
phenomena are not induced by event-related potentials; the ERP dies out after 400 ms, and is thus too transient to account for the robust amplitude modulation we observe. Furthermore, the ISI periods had smaller or no ERPs, and exhibited dramatically larger modulation. Sharp discontinuities in the timeseries can give artifactual phase modulation at higher frequencies, so artifactual epochs had to be excluded from analysis. When the method was applied to task-modulated brown noise (Figure 9), there was no coupling, suggesting that coupling is not a by-product of the method used for analysis.

**TECHNICAL CONSIDERATIONS**

The techniques presented here for characterizing and statistically testing phase and amplitude interactions in the cortical surface potential are performed in stages, each of which is non-trivial. We independently isolate a broadband signal and simultaneous brain rhythms; subsequently, we examine correlations between these two phenomena. In order to test whether our assumptions about the underlying mechanisms could be valid, we constructed a simulated signal that had task-related broadband change, and was modulated by rhythmic influence in a task-dependent way (Figure 8). Our analytic algorithms were able to naively uncover the broadband change as well as the rhythmic modulation. These phenomena are not induced by event-related potentials; the ERP dies out after 400 ms, and is thus too transient to account for the robust amplitude modulation we observe. Furthermore, the ISI periods had smaller or no ERPs, and exhibited dramatically larger modulation. Sharp discontinuities in the timeseries can give artificial phase modulation at higher frequencies, so artifactual epochs had to be excluded from analysis. When the method was applied to task-modulated brown noise (Figure 9), there was no coupling, suggesting that coupling is not a by-product of the method used for analysis.

**SUPPRESSION BY SYNCHRONIZATION**

Existing studies of rhythm-broadband modulations have mainly focused on a facilitatory role (Womelsdorf et al., 2005; Canolty et al., 2006; Jensen and Colgin, 2007; Siegel et al., 2008; He et al., 2010), suggesting that the presence of a rhythm enables an active component of local cortical processing. While this may be the case for
These observations have been linked to the hypothesis that rhythms enhance spike transmission between synchronized areas—“communication through coherence” (Singer, 1993; Fries, 2005). This is consistent with the increase in power that we observe in γ-rhythms (Figures 4H, I). We propose that rhythms may also play a role in suppressing local cortical computation, with the cortically suppressed (disengaged) state one in which widespread populations

θ-range modulations, including those observed here, the β-range changes we observe are more suggestive of an inhibitory process in which the rhythm actively modulates local occipital cortical activity during periods of task disengagement (Handel et al.; Klimesch et al., 2007). In the setting of the γ-rhythm, it has been demonstrated that the influence of the rhythm facilitates cortical computation (Womelsdorf et al., 2007), particularly during visual processing.

Figure 4 | Coupling across occipital cortex, in subject 5, with a focus on the β-range (12–20 Hz). (A–G) Each of seven surface electrodes is shown on an electrode strip beginning in medial, peri-calcarine, occipital cortex, extending laterally around the occipital pole into the lateral occipital gyrus. The left-most series of bars in each panel is the log-broadband amplitude, in Z-score units, with the mean of ISI periods subtracted out. Errorbars represent 3 SEM. The right-most error bars, flanking the horizontal origin, represent the variation during ISI periods. The medial 4 and the most lateral electrodes [e.g., (A–D), (G)] all show increased local cortical activity during visual search, while the 5th and 6th electrode sites show suppressed activity during visual search (these two share gyrual location). The palettes show average coupling across all cues. All sites have strong and significant coupling to the 12–20 Hz (β) range. The upper-right axes within each panel show the amplitude of the 12–20 Hz rhythm during different cue types. There is a lower amplitude during visual search engagement in every case. The 12–20 Hz modulation of broadband amplitude, however, is selectively suppressed during task engagement in the (B)–(D) sites, which share common gyrual location. (H) Dynamics of visual response from the electrode highlighted in (A). On the Left: The upper trace is the average event-related broadband (ERBB) for each of the cue types. The middle plot is the average dynamic spectrum for all active sites combined called the “event-related spectral perturbation” (ERSP). The lower plot is the event-related potential (ERP) for each cue type. On the right, the changes in the mean spectrum during visual search (red) and ISI (blue) are shown. Note the so-called “event-related desynchronization” in the α/β rhythm range, and “event-related synchronization” in the γ-range (Pfurtscheller, 1999). Broadband change, though small, is present throughout – although it is covariant with the γ-rhythm change, it is a distinct entity. (I) Same analysis as in (H), for the electrode highlighted in (D). Broadband change is strong and robust, with α/β-ERD and γ-ERS. In this case, the broadband change is large compared with the γ-rhythm ERS, although both can still be seen. The change at this site was representative of all three occipital pole electrodes – sites (B)–(D). 

(J) Inter-electrode phase coherence in the 12–20 Hz range. (K) Inter-electrode amplitude correlation in the 12–20 Hz range.
Figure 5 | The variety of dynamics of occipital visual response, and the different changes of rhythms: Phase modulation of cortical activity can both increase and decrease with task engagement. (A) Dynamics are examined from four electrodes (color coded) in subject 1. (B) Pink electrode site dynamics – posterior lower bank of the calcarine sulcus. The three panels on the left show the average dynamics leading into the 2-s visual search cues (onset at time zero). The upper trace is the average event-related broadband (ERBB) for each of the cue types. The middle plot is the average dynamic spectrum for all active sites combined – the “event-related spectral perturbation” (ERSP). The lower plot is the event-related potential (ERP) for each cue type. (C) The coupling palette for the pink electrode site. Note the strong θ and β contributions. (D) Broadband activity during each of the different cue types. The log-broadband amplitude is shown, in Z-score units, with the mean of ISI periods subtracted out. Errorbars represent 3*SEM. The right-most error bars, flanking the horizontal origin, represent the variation during ISI periods. (E) Upper panel: 4–8 Hz amplitude during each of the different cue types. Lower panel: The modulation of the broadband by the 4–8 Hz phase during each cue type. (F) As in (E), for 12–20 Hz. (G) Interaction between rhythms, computed analogously to the rhythm-broadband interaction. The 4–8 Hz phase modulation of the 12–20 Hz amplitude is quantified, revealing a significant coupling during all but the “rightward” cue condition. (H) As in (B)–(G), for the green electrode site – lingual gyrus. There is a suppression of broadband activity when engaged in visual search, revealed by the broadband timeseries and mean broadband amplitude (but not by the ERP). Broadband amplitude changes couple to both the 4–8 Hz rhythm and the 12–20 Hz rhythm. There is a specific augmentation of the 12–20 Hz rhythm amplitude and 12–20 Hz coupling to the broadband rhythm during engagement in the visual task. The interaction between the two rhythms is significant during the “rightward” cue. (I) As in (B)–(G) for the black electrode site – posterior lateral occipitotemporal gyrus. There is specific broadband power increase at time of cue onset – the bars show that this is only sustained for the “leftward” cue. There is task-related increase in the 4–8 Hz rhythm amplitude and corresponding coupling. The 12–20 Hz rhythm shows a task-related decrease in both amplitude and coupling during visual search. The right-most plot demonstrates that there is significant modulation of the 12–20 Hz amplitude by the 4–8 Hz phase. (J) As in (B)–(G) for the yellow electrode site – anterior lower bank of the calcarine sulcus. Visual search cues show increase in broadband, 4–8 Hz, and 12–20 Hz amplitude. There is also a task-related increase in modulation of the broadband amplitude by 4–8 Hz and 12–20 Hz phase. In turn, the 12–20 Hz amplitude is modulated by the 4–8 Hz phase, specifically while engaged in the visual search cues, and not during the ISI cues.
of cortical neurons are phase-coupled to the rhythm (Figure 7). In this "suppression-by-synchronization" model, neurons from a distant "pacemaker" circuit project diffusely to populations of cortical pyramidal neurons, targeting their basal dendrites and somas with synchronized input. Whether the synchronized inputs are excitatory or inhibitory, the cortico-cortical inputs between pyramidal neurons will need to be stochastically resonant with the synchronized input to induce a downstream action potential (anti-aligned if the synchronizing input is inhibitory, aligned if it is excitatory). In this way, weak but synchronous input keeps the population in a "dynamically suppressed" state, where it can quickly transition into an engaged "processing state." An alternative model – suppression by blanket inhibition, would be more metabolically expensive and would also not allow for easy transition from the suppressed state to a computing state because the targeted pyramidal population would have to overcome an effective hyperpolarization barrier. In the suppression-by-synchronization regime, one need only remove time-locking influence and the neuronal population can switch to an engaged and actively computing state. At this stage, identifying the anatomic locus of the synchronizing source will require further
research. The thalamus, specifically the lateral pulvinar and lateral geniculate nucleus, is a compelling candidate because of its diffuse projection and known role in visual processing (Zhang et al., 2010). Additionally, it has been demonstrated that weak but synchronous thalamic input can drive cortical processing dramatically in the active feedforward state (Bruno and Sakmann, 2006). Whatever the case, this rhythmic modulatory influence acts over large cortical regions, and coherence is significantly decreased during visual engagement (Figure 4J). Perhaps the same is true for selective suppression of other cortical regions. During behavior, some rhythms
might serve as “spotlights of utility” that, at baseline, actively suppress non-relevant cortical areas by synchronization. When the cortical area becomes functionally relevant the rhythm is withdrawn.

**UNIVERSAL RHYTHMIC MOTIFS?**

Although it is frequently treated as if a rhythm at a particular frequency has a universal functional property, a rhythm with a particular center frequency need not serve a single neural function in every state and location in which it is observed. The fact that we observe different preferred phases, and also conjugate task-related changes in the same frequency ranges, in different cortical areas, suggests that there is unlikely to be a simple, universal, role for a particular band-limited rhythm. What we call “β” in the lateral occipital gyrus and what we call “β” at the occipital pole may in fact represent different phenomena, with different physiological origins, but with a common timescale and corresponding frequency range (Figure 4). That said, the observation of significant changes in inter-electrode coherence between adjacent electrodes suggests a common etiology that selectively releases some cortical areas (e.g., sites Figures 4A–D,G) but not others (sites Figures 4E,F), in a gyrally-conserved way, during task engagement.

The fact that the phase–amplitude coupling motifs sometimes shift substantially in phase across subjects or electrodes might point to different types of physiologic phenomena which are revealed with different types of rhythmic coupling motifs. For example, a rhythm with one preferred phase might exert an excitatory influence via one class of channels, and a different rhythm might exert an inhibitory influence via a separate class of channels. The different timescales implied by the frequencies different rhythmic phenomena might reflect feedback loops involving different numbers of neurons, or slow versus fast types of membrane channels. Some rhythms might reflect emergent properties of highly interconnected networks, while other rhythms of the same frequency range but different cortical location, might reflect cortical-subcortical feedback loops.

**REFERENCES**


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**METHODOLOGICAL APPENDIX**

**SIGNAL PRE-PROCESSING**

To reduce common artifact, the potential, \( V_n(t) \), measured at each electrode \( n \) was re-referenced with respect to the common average of all electrodes, \( V(t) = V_n(t) - 1/N \sum_{n=1}^{N} V_n(t) \), (channel label, \( n \), henceforth dropped). Electrodes with significant artifact or epileptiform activity were rejected prior to common averaging. Epochs that appeared artifactual were rejected. Following re-referencing, only occipital electrodes were further examined; the remainder was discarded. Ambient line noise was rejected by notch filtering between 58 to 62 Hz using a 3rd-order Butterworth filter (Porat, 1997).

**POWER SPECTRAL DENSITIES**

**Power spectral snapshots**

A set of epochs surrounding onset and middle of each visual search and ISI cue, \( \tau_q \), were extracted from \( V(t) \); each epoch was of duration \( T = 1 \) s, \( (\tau_q - (1/2)T) < t < (\tau_q + (1/2)T) \). The epochs were sorted according to cue type \( q \), and labeled by their event markers \( \tau_q \) [note times of onset, middle of both cues and ISI]. The power spectral density (PSD) of the epoch flaming time \( \tau_q \) was calculated as:

\[
P(f,q) = \frac{1}{\sqrt{T}} \int_{\tau_q - T/2}^{\tau_q + T/2} V(t)H(t)e^{j2\pi ft} dt
\]

with Hann window (Porat, 1997)

\[
H(t) = \frac{1}{2} \left( 1 - \cos \left( \frac{2\pi t}{T} \right) \right)
\]

**DYNAMIC POWER SPECTRAL MEASURES**

Time-frequency approximations (dynamic spectra) were made using both a wavelet and a Hilbert transform approach.

**Wavelet approach**

A Morlet wavelet (Goupillaud et al., 1984) of the form:

\[
\psi(t) = \exp(2\pi i ft) \exp(-t^2/2\sigma^2)
\]

was convolved with the timseries to get a time-frequency estimate for each \( f = 1/T \):

\[
\tilde{V}(f,\tau) = \sum_{t'=T/2}^{T/2} V(t+t')\psi(t',\tau)
\]

A total of 5 cycles (5\( \pi \)) was used to estimate the amplitude and phase of the signal at each frequency for every point in time. In this way a time-varying Fourier component \( \tilde{V}(f,\tau) = r(f,\tau) e^{j\phi(f,\tau)} \), with fixed uncertainty between the confidence in the estimate of the instantaneous amplitude and phase versus the confidence in temporal resolution is obtained at each Hz.

**Hilbert transform approach**

A complex signal to reflect the timecourse of a functionally relevant frequency-range band was constructed as follows: The signal \( V(t) \) was band-passed using a 3rd-order Butterworth filter for a specific range, to obtain the “band-limited” potential, \( V(F,t) \), where \( F \) denotes the frequency range (e.g., for “alpha,” \( F \rightarrow [8–12] \) Hz, etc.). A complex analytic signal, \( \tilde{V}(F,t) = V(F,t) + iV^{\text{HM}}(F,t) \) was constructed using the Hilbert transform (e.g., such that the new signal satisfies the Cauchy-Riemann conditions for analyticity at all times).

**Discrete-time signal processing**

This signal may also be expressed in polar notation:

\[
\tilde{V}(F,t) = r(F,t) e^{j\phi(F,t)}
\]

The “analytic amplitude” of the range \( F \) at time \( t \) is \( r(F,t) \) and the “phase” is \( \phi(F,t) \). The interpretation of \( \phi \) is intuitively difficult, but the most concrete understanding is that the rhythm captured by range \( F \) is most surface-positive at \( \phi = 0 \), and most surface-negative at \( \phi = \pi \) or \( -\pi \). Note that \( \phi \) becomes poorly defined as \( r \rightarrow 0 \). For discussion of different approaches and illustration of nested ECoG measurements, see, for example, Penny et al. (2008).

**AMPLITUDE CORRELATION AND PHASE COHERENCE OF RHYTHMS**

The relationships between complex rhythms \( \tilde{V}_n(F, t) = r_n(F, t) e^{j\phi_n(F, t)} \) for trial \( k \) (electrode \( n \)) were determined as follows. The inter-electrode amplitude correlation \( R_{ab}(k) \) for the rhythm defined by range of frequencies \( F \) between electrodes \( a \) and \( b \), during trial \( k \) is:

\[
R_{ab}(k) = \frac{1}{T_k} \sum_{t=1}^{T_k} \frac{r_a(F, t_k) - \langle r_a(F, t_k) \rangle}{\sigma_{r_a(F, t_k)}}\frac{r_b(F, t_k) - \langle r_b(F, t_k) \rangle}{\sigma_{r_b(F, t_k)}}
\]

Where \( t_k \) are the times of epoch \( k (t_k \in k, \text{total } T_k \text{ timepoints}) \) and the z-score amplitude for the epoch is:

\[
\langle r_a(F, t_k) \rangle = \frac{1}{T_k} \sum_{t=1}^{T_k} r_a(F, t_k)
\]

\[
\sigma_{r_a(F, t_k)} = \left( \frac{1}{T_k} \sum_{t=1}^{T_k} \left( r_a(F, t_k) - \langle r_a(F, t_k) \rangle \right)^2 \right)^{1/2}
\]

The single trial inter-electrode phase coherence, \( Q_{ab}(k) \), is:

\[
Q_{ab}(k) = \frac{1}{T_k} \sum_{t=1}^{T_k} \left| \frac{\tilde{V}_a(F, t_k + \tau_a) \tilde{V}_b(F, t_k + \tau_b)}{\left| \tilde{V}_a(F, t_k) \tilde{V}_b(F, t_k) \right|} \right|
\]

**STIMULUS-TRIGGERED AVERAGE OF TIME-FREQUENCY POWER ESTIMATE**

This time-frequency approximation can be used to calculate mean power in relation to the onset of visual stimuli:

\[
P_s^x(f, t_s) = \frac{1}{N_s} \sum_{t=t_s}^{t_s + T_s} \left| \frac{\tilde{V}(f, t_s + \tau)}{\tilde{V}(f, t')^2} \right|
\]

Where \( \tau \) denote onset times of visual search cues (total \( N_s \)), and \( t' \) denote inter-stimulus times (total \( N_t \)). The peristimulus time window of interest is denoted \( t_s \); in our case, \(-1s < t_s < 3s \). These normalized maps of power as a function of time and frequency provide important information about characteristic spectral changes with local cortical function (also called “event-related spectral perturbations” – ERSPs; Makeig et al., 2002). While ERSPs could be
calculated independently for each condition (arrow direction) of the visual search task, for simplicity we calculate an ERSP collapsed across conditions.

**DECOUPLING THE CORTICAL SPECTRUM TO SEPARATE RHYTHMIC ACTIVITY AWAY FROM BROADBAND CHANGE**

The decoupling process is described and illustrated in detail in the main text and supplement to Miller et al. (2009c). It was applied here as follows:

**Principal component decomposition of spectral change**

The samples of the PSD, $P(f, q)$, (total $N_q$), were normalized prior to decomposition.

$$\hat{P}(f, q) = \ln(P(f, q)) - \ln \left( \frac{1}{N_q} \sum_q P(f, q) \right)$$

The PCA method (Jolliffe, 2002) determines the eigenvalues $\hat{\lambda}_i$ and eigenvectors $\hat{\varphi}_i$ of the correlation matrix:

$$C(f, f^\prime) = \sum_q P(f, q) \hat{P}(f^\prime, q)$$

These eigenvectors, $\hat{C} \hat{\varphi}_i = \lambda_i \hat{\varphi}_i$, the “Principal Spectral Components” (PSCs), reveal which frequencies vary together, and are ordered by magnitude of corresponding eigenvalue: $\lambda_1 > \lambda_2 > \ldots > \lambda_{N_q}$ ($N_q$ number of frequencies). If we define the rotation matrix $\hat{A}(f, k) = (\hat{\varphi}_1, \hat{\varphi}_2, \ldots, \hat{\varphi}_{N_q})$, then the projection,

$$W(k, q) = \sum_f \hat{A}(f, k) \hat{P}(f, q)$$

The inverse rotation matrix $\hat{A}^{-1}$, $\hat{A}^{-1} \hat{A} = \hat{I}$, allows us to compare and visualize specific subsets of PSC components with the original full spectrum in frequency space. The 2nd to 4th PSCs typically capture rhythmic power spectral phenomena, and power spectra can be reconstructed with and without this rhythmic influence:

$$\hat{P}_s(f, q) = \sum_{k \in \Sigma} \hat{A}^{-1}(f, k) W(k, q)$$

If the 2nd to 4th PSCs are omitted, $\Sigma \rightarrow \{1, 5, \ldots N\}$, then PSDs can be reconstructed where changes in rhythmic spectral phenomena are mostly removed (although there may be residual variance in the decomposition, or some rhythmic influence in all cases). If $\Sigma \rightarrow \{2, 4\}$, then PSDs can be reconstructed where changes in rhythmic spectral phenomena are mostly isolated (Figures 1C and 7).

**The timecourse of broadband spectral change**

The time-dependent, normalized, dynamic spectrum, $\hat{P}(f, q)$, can be obtained in parallel fashion to the spectral snapshots.

$$P(f, t) = \frac{1}{N_q} \sum_q \hat{P}(f, q)$$

and

$$\hat{P}(f, t) = \ln(P(f, t)) - \ln \left( \frac{1}{N_q} \sum_q P(f, t) \right).$$

The reflection of the 1st PSC ($\hat{\varphi}_1$) in the dynamic spectrum can be estimated by projecting the dynamic spectrum onto it.

$$\ln A(t) = \sum_f \varphi(f) P(f, t)$$

We call it $\ln A(t)$ here, because it approximates the logarithm of the timecourse of the coefficient of a power-law in the cortical spectrum of the form $P(f, t) = A(t) f^{-\alpha}$ (Miller et al., 2009b); it is smoothed with a Gaussian window of 50 ms standard deviation, z-scored, and exponentiated to obtain the “broadband” traces of Figures 1D, 4H, I and 5B, H–J (e.g., time-varying estimates of the coefficient of the power-law spectrum). The broadband power timecourses are robust estimates of behaviorally relevant local cortical activity (Miller et al., 2009c). Because the quantity $\ln A(t)$ is approximately log-normal distributed, we express it in z-score units, and, for notational brevity, denote it $\chi(t)$ in connection to the broadband power-law it reflects.

**SYNTHETIC DATA (FIGURE 8)**

The heuristic method illustrated in Figures 7A–C was used to create simulated data by combining input signals whose properties are known. The synthetic data could then be analyzed to validate the methods developed for the cortical data. The process is an extension of the one used to illustrate broadband, power-law, spectral change in previous manuscripts (Bedard et al., 2006; Miller et al., 2009b; Miller, 2010). Recent in vivo simultaneous recordings have demonstrated a strong correlation between trans-membrane and local field potentials (Okun et al., 2010), suggesting that models like this, based upon a relationship between post-synaptic potentials and field potential, may provide useful insight. It is a construct that simulates the hypothesis of Figures 7A–C, which is a mechanism for what role some (not all) rhythms might play in cortical processing. This heuristic is meant to synthetically generate data of known 1/broadband structure with influence of nested oscillation. It is not meant to serve as an accurate physiological model, but rather as a means to validate our signal processing techniques on synthetic data that has approximately similar statistics as empirical data, but with known underlying structure. They are synthesized in the following steps:

**Step 1: Action potentials (AP~“spikes”) with Poisson-distributed inter-spike intervals arrive from a pre-synaptic cortical pyramidal neuron.** We model 6000 of these and assign a random synaptic weight within the interval –1 to 1 to each synapse. The instantaneous AP rate, $\bar{\varphi}_u$, is modulated as a function of task, so that the probability of an AP is higher during the simulated visual search time. This can be formalized as:

$$\varphi_u(t) = \begin{cases} 1 & \eta < \rho(t) \\ 0 & \eta > \rho(t) \end{cases}$$

where $\eta$ is a random variable uniformly distributed on the interval [0, 1] and $\rho(t)$ is a variable threshold that corresponds to the mean population spike rate within the $k$th epoch (e.g., $\rho(t)$ = “firing rate”/“sampling rate”). The maximum firing rate was set to 40 spikes/s. During simulated ISI epochs, $\rho(t)$ was set to 25% of maximum firing rate, and during each simulated visual search epoch the value of $\rho(t)$ was set to a value drawn from a uniform distribution on the range 55–100% of maximum firing rate.
Step 2: Each AP produces stereotyped transient post-synaptic current with a sharp rise, and an exponential decay of timescale \( \tau_s = (2\pi75 \text{ Hz})^{-1} = 2.1 \text{ ms} \) consistent with empirical measurement (Sabatini and Regehr, 1996). Following Lindén et al. (2010), the timecourse of the synaptic current induced by a single AP is:

\[ I_s(t) = \eta(t/\tau_s)e^{-(t-\theta(t))}/\tau_s \]

where \( \eta \), in this case, is a “synaptic strength” drawn randomly from a uniform distribution on the range \([-1, 1]\), \( \tau_s \) is the time constant of the synapse, and \( \theta(t) \) is a step function (i.e., “Heavyside function”). The AP timeseries is convolved (* denotes convolution operation) with the synaptic current shape, \( I_s \).

\[ \sigma_m = \sigma_m^3 * I_s \]

Step 3: Synaptic inputs from 6000 synapses, “m,” are summed at each point in time:

\[ W(t) = \sum_m \sigma_m(t) \]

and charge integrates over time, perturbing the trans-membrane difference in charge concentration between the inside and outside of the neuron (Connor and Stevens, 1971).

Step 4: The temporal integration and Ohmic leakage that produce the broadband \( B(t) \) are governed by:

\[ \frac{d B(t)}{dt} = -\alpha B(t) + W(t). \]

The timecourse of \( B(t) \) is determined iteratively. Note that, in more comprehensive and subtle simulations, the effect of rhythmic input (through back-propagation or otherwise), might be incorporated into this step.

Step 5: A cortical rhythm \( \zeta(t) = r_z(t) \cos(2\pi f_\theta t + \Delta(t_z)) \), is simulated, with center frequency \( f_\theta \) set to 15 Hz. The amplitude \( r_z(t) \) is set to zero during simulated visual search epochs, and takes on a non-zero value drawn randomly from a uniform non-zero distribution during ISI epochs (determining the strength of the modulation). A different random phase shift, \( \Delta(t_z) \), is also added to each epoch to prevent inter-trial coherence in the mean spectrogram. This rhythm contributes to the simulated membrane potential of a neuron in two ways. Firstly, it multiplicatively modulates the broadband process:

\[ V_{bb}(t) = (1 + \zeta(t))B(t) \]

Secondly, the rhythm contributes directly to the potential:

\[ V_z(t) = A_s r_z(t) \cos(2\pi f_\theta t + \Delta(t_z) + \phi), \]

where \( \phi \) is the coupling phase (which we set to \( \pi/4 \)), and \( A_s \) is the overall amplitude of the rhythmic contribution, linked to match the variation in the underlying noise: \( A_s = A_s^0 \sigma_{\text{sim}}/(\sigma_{\text{sim}} + \sigma_{\text{data}}) \) and \( \sigma \) denotes the standard deviation over time, and \( V_{bb}(F, t) \) is the band-pass filtered \( V_{bb}(t) \) for \( F = \{f_\theta - 2 \text{ Hz to } f_\theta + 2 \text{ Hz} \} \). Then the simulation contribution to the potential from one neuron is \( V_{bb}(t) + V_z(t) \). In this simulation, we use this quantity to approximate the timecourse that gives rise to our measured potential.

Step 6: Simulation is performed for the summation of 10 such model neurons. The broadband change is a stochastic process, different in each neuron although the timecourse of firing probability, \( r_z(t) \), is the same at each synapse, and in each neuron. The timing and phase of the rhythm is also fixed across neurons (because it is “synchronized”). The resulting timeseries was analyzed in the same manner as the cortical data were.

The inhibition through synchronization aspect of the model is forced into effect by having the firing rate, \( \rho(t_z) \), constructed to be low when \( r_z(t) \) is non-zero, and \( \rho(t_z) \) high as \( r_z(t) \to 0 \). More sophisticated network simulations should exhibit this as an emergent property.

**NEGATIVE CONTROL VALIDATION ON BROWN NOISE (FIGURE 9)**

We tested the methods on pure brown noise that was generated by creating timeseries with property \( P(f) = f^{-2} \) by taking a random white noise variable \( \eta \) uniformly distributed on the interval \([-0.25, 0.25]\) during simulated ISI, and \([1, 1]\) during simulated visual engagement. It was then temporally integrated to give it brown noise structure, and high-passed at 1 Hz to avoid DC offsets. Analysis was then performed in an identical manner as with data and the above simulation to demonstrate a negative control (Figure 9).